## Mathematics

## Grade 3

## PA Alternate Eligible Content

## PA Reporting Category: M03.A-T Numbers and Operations in Base Ten

## PA Core Standards:

CC.2.1.3.B. 1 Apply place-value understanding and properties of operations to perform multi-digit arithmetic.

## ASSESSMENT ANCHOR

M03.A-T. 1 Use place-value understanding and properties of operations to perform multi-digit arithmetic.

| DESCRIPTOR | ELIGIBLE CONTENT | Alternate Eligible <br> Content Code | ALTERNATE ELIGIBLE CONTENT |
| :--- | :--- | :--- | :--- |
| M03.A-T.1.1 <br> Apply place-value <br> strategies to solve <br> problems. | M03.A-T.1.1.1 <br> Round two- and three-digit whole numbers to the <br> nearest ten or hundred, respectively. | M03AT1.1.1a | Round a two-digit number to the nearest <br> ten |
|  | M03.A-T.1.1.2 <br> Add two- and three- digit whole numbers (limit sums <br> from 100 through 1,000) and/or subtract two- and <br> three-digit numbers from three-digit whole numbers. | M03AT1.1.2b | Demonstrate understanding subtraction <br> with small sets |
|  | M03.A-T.1.1.3 <br> Multiply one-digit whole numbers by two-digit <br> multiples of 10 (from 10 through 90). | Demonstrate understanding of addition <br> with small sets |  |
|  | M03.A-T.1.1.4 <br> Order a set of whole numbers from least to greatest or <br> greatest to least (up through 9,999, and limit sets to <br> no more than four numbers). | M03AT1.1.4a | Order 3 numbers under 10 |

## PA Reporting Category: M03.A-F Numbers and Operations - Fractions

## PA Core Standards:

CC.2.1.3.C. 1 Explore and develop an understanding of fractions as numbers.

## ASSESSMENT ANCHOR

M03.A-F. 1 Develop an understanding of fractions as numbers.

| DESCRIPTOR | ELIGIBLE CONTENT | Alternate Eligible Content Code | ALTERNATE ELIGIBLE CONTENT |
| :---: | :---: | :---: | :---: |
| M03.A-F.1.1 <br> Develop and apply number theory concepts to compare quantities and magnitudes of fractions and whole numbers. | M03.A-F.1.1.1 <br> Demonstrate that when a whole or set is partitioned into $y$ equal parts, the fraction $1 / y$ represents 1 part of the whole and/or the fraction $x / y$ represents $x$ equal parts of the whole (limit denominators to 2, 3, 4, 6, and 8; limit numerators to whole numbers less than the denominator; and no simplification necessary). | M03AF1.1.1a | Identify the unit fraction or other proper fraction (denominators $=2$, $3,4,6$ ) that matches the representation |
|  | M03.A-F.1.1.2 <br> Represent fractions on a number line (limit denominators to 2, 3, 4, 6, and 8; limit numerators to whole numbers less than the denominator; and no simplification necessary). |  |  |
|  | M03.A-F.1.1.3 <br> Recognize and generate simple equivalent fractions (limit the denominators to $1,2,3,4,6$, and 8 and limit numerators to whole numbers less than the denominator). <br> Example 1: $1 / 2=2 / 4$ <br> Example 2: $4 / 6=2 / 3$ | M03AF1.1.3b | Identify equivalent fractions using representations |
|  | M03.A-F.1.1.4 <br> Express whole numbers as fractions, and/or generate fractions that are equivalent to whole numbers (limit denominators to $1,2,3,4,6$, and 8 ). <br> Example 1: Express 3 in the form $3=3 / 1$. <br> Example 2: Recognize that $6 / 1=6$. |  |  |
|  | M03.A-F.1.1.5 <br> Compare two fractions with the same denominator (limit denominators to $1,2,3,4,6$, and 8 ), using the symbols $>,=$, or <, and/or justify the conclusions. |  |  |

## PA Reporting Category: M03.B-O Operations and Algebraic Thinking

## PA Core Standards:

CC.2.2.3.A. 1 Represent and solve problems involving multiplication and division.

## ASSESSMENT ANCHOR

M03.B-O. 1 Represent and solve problems involving multiplication and division.

| DESCRIPTOR | ELIGIBLE CONTENT | Alternate Eligible Content Code | ALTERNATE ELIGIBLE CONTENT |
| :---: | :---: | :---: | :---: |
| M03.B-O.1.1 <br> Understand various meanings of multiplication and division. | M03.B-O.1.1.1 <br> Interpret and/or describe products of whole numbers (up to and including $10 \times 10$ ). <br> Example 1: Interpret 35 as the total number of objects in 5 groups, each containing 7 objects. <br> Example 2: Describe a context in which a total number of objects can be expressed as $5 \times 7$. | M03BO1.1.1a | Use a model in a multiplication situation |
|  | M03.B-O.1.1.2 <br> Interpret and/or describe whole-number quotients of whole numbers (limit dividends through 50 and limit divisors and quotients through 10). <br> Example 1: Interpret $48 \div 8$ as the number of objects in each share when 48 objects are partitioned equally into 8 shares, or as a number of shares when 48 objects are partitioned into equal shares of 8 objects each. <br> Example 2: Describe a context in which a number of shares or a number of groups can be expressed as $48 \div 8$. |  |  |
| M03.B-O.1.2 <br> Solve mathematical and real-world problems using multiplication and division, including determining the missing number in a multiplication and/or division equation. | M03.B-O.1.2.1 <br> Use multiplication (up to and including $10 \times 10$ ) and/or division (limit dividends through 50 and limit divisors and quotients through 10) to solve word problems in situations involving equal groups, arrays, and/or measurement quantities. |  |  |
|  | M03.B-O.1.2.2 <br> Determine the unknown whole number in a multiplication (up to and including $10 \times 10$ ) or division (limit dividends through 50 and limit divisors and quotients through 10) equation relating three whole numbers. <br> Example: Determine the unknown number that makes an equation true. |  |  |

## PA Reporting Category: M03.B-O Operations and Algebraic Thinking

## PA Core Standards:

CC.2.2.3.A. 2 Understand properties of multiplication and the relationship between multiplication and division.

## ASSESSMENT ANCHOR

M03.B-O. 2 Understand properties of multiplication and the relationship between multiplication and division.

| DESCRIPTOR | $\quad$ ELIGIBLE CONTENT | Alternate Eligible <br> Content Code | ALTERNATE ELIGIBLE CONTENT |
| :--- | :--- | :--- | :--- |
| M03.B-O.2.1 <br> Use properties to <br> simplify and solve <br> multiplication problems.M03.B-O.2.1.1 <br> Apply the commutative property of multiplication (not <br> identification or definition of the property). | M03.B-O.2.1.2 <br> Apply the associative property of multiplication (not <br> identification or definition of the property). |  |  |
| M03.B-O.2.2 <br> Relate division to a <br> missing-number <br> multiplication equation. | M03.B-O.2.2.1 <br> Interpret and/or model division as a multiplication equation <br> with an unknown factor. <br> Example: Find $32 \div 8$ by solving $8 \times ?=32$. |  |  |

## PA Reporting Category: M03.B-O Operations and Algebraic Thinking

## PA Core Standards:

CC.2.2.3.A. 4 Solve problems involving the four operations, and identify and explain patterns in arithmetic.

## ASSESSMENT ANCHOR

M03.B-O. 3 Solve problems involving the four operations, and identify and explain patterns in arithmetic.

| DESCRIPTOR | ELIGIBLE CONTENT | Alternate Eligible Content Code | ALTERNATE ELIGIBLE CONTENT |
| :---: | :---: | :---: | :---: |
| M03.B-O.3.1 <br> Use operations, patterns, and estimation strategies to solve problems (may include word problems). | M03.B-O.3.1.1 <br> Solve two-step word problems using the four operations (expressions are not explicitly stated). Limit to problems with whole numbers and having whole-number answers. | M03BO3.1.1a | Solve a 1-step real-world problem involving numbers under 10 using addition or subtraction |
|  | M03.B-O.3.1.2 <br> Represent two-step word problems using equations with a symbol standing for the unknown quantity. Limit to problems with whole numbers and having whole-number answers. |  |  |
|  | M03.B-O.3.1.3 <br> Assess the reasonableness of answers. Limit problems posed with whole numbers and having whole-number answers. |  |  |
|  | M03.B-O.3.1.4 <br> Solve two-step equations using order of operations (equation is explicitly stated with no grouping symbols). |  |  |
|  | M03.B-O.3.1.5 <br> Identify arithmetic patterns (including patterns in the | M03BO3.1.5a | Identify a mathematical pattern in a real-world problem |
|  | addition table or multiplication table) and/or explain them using properties of operations. <br> Example 1: Observe that 4 times a number is always even. Example 2: Explain why 6 times a number can be decomposed into three equal addends. | M03BO3.1.5b | Identify the 3 next terms in a mathematical pattern (increasing by 2, 5 or 10) |
|  | M03.B-O.3.1.6 <br> Create or match a story to a given combination of symbols (+, -, x, $\div,<,>$, and $=$ ) and numbers. |  |  |
|  | M03.B-O.3.1.7 <br> Identify the missing symbol (+,,$- \times, \div,<,>$, and $=$ ) that makes a number sentence true. |  |  |

## PA Reporting Category: M03.C-G Geometry

## PA Core Standards:

CC.2.3.3.A. 1 Identify, compare, and classify shapes and their attributes.
CC.2.3.3.A. 2 Use the understanding of fractions to partition shapes into parts with equal areas and express the area of each part as a unit fraction of the whole.

## ASSESSMENT ANCHOR

M03.C-G. 1 Reason with shapes and their attributes.

| DESCRIPTOR | ELIGIBLE CONTENT | Alternate Eligible <br> Content Code | ALTERNATE ELIGIBLE CONTENT |
| :--- | :--- | :--- | :--- |
| M03.C-G.1.1 <br> Analyze characteristics <br> of polygons. | M03.C-G.1.1.1 <br> Explain that shapes in different categories may share <br> attributes and that the shared attributes can define a larger <br> category. <br> Example 1: A rhombus and a rectangle are both <br> quadrilaterals since they both have exactly four sides. <br> Example 2: A triangle and a pentagon are both polygons <br> since they are both multi-sided plane figures. | M03CG1.1.1a <br> polygons |  |
|  | M03.C-G.1.1.2 <br> Recognize rhombi, rectangles, and squares as examples of <br> quadrilaterals and/or draw examples of quadrilaterals that <br> do not belong to any of these subcategories. |  | Partition a rectangle into parts with <br> equal areas |
|  | M03.C-G.1.1.3 <br> Partition shapes into parts with equal areas. Express the <br> area of each part as a unit fraction of the whole. <br> Example 1: Partition a shape into 4 parts with equal areas. <br> Example 2: Describe the area of each of 8 equal parts as 1/8 <br> of the area of the shape. | M03CG1.1.3a |  |

## PA Reporting Category: M03.D-M Measurement and Data

## PA Core Standards:

CC.2.4.3.A. 1 Solve problems involving measurement and estimation of temperature, liquid volume, mass or length.
CC.2.4.3.A. 2 Tell and write time to the nearest minute and solve problems by calculating time intervals.
CC.2.4.3.A. 3 Solve problems and make change involving money using a combination of coins and bills.

## ASSESSMENT ANCHOR

M03.D-M. 1 Solve problems involving measurement and estimation of intervals of time, money, liquid volumes, masses, and lengths of objects.

| DESCRIPTOR | ELIGIBLE CONTENT | Alternate Eligible Content Code | ALTERNATE ELIGIBLE CONTENT |
| :---: | :---: | :---: | :---: |
| M03.D-M.1.1 <br> Determine or calculate time and elapsed time. | M03.D-M.1.1.1 <br> Tell, show, and/or write time (analog) to the nearest minute. | M03DM1.1.1a | Tell time to the hour or half hour on a clock |
|  | M03.D-M.1.1.2 <br> Calculate elapsed time to the minute in a given situation (total elapsed time limited to $\mathbf{6 0}$ minutes or less). |  |  |
| M03.D-M.1.2 <br> Use the attributes of liquid volume, mass, and length of objects. | M03.D-M.1.2.1 <br> Measure and estimate liquid volumes and masses of objects using standard units (cups [c], pints [pt], quarts [qt], gallons [gal], ounces [oz.], and pounds [lb]) and metric units (liters [I], grams [g],and kilograms [kg]). | M03DM1.2.1a | Identify and use the appropriate measurement tool based on the situation |
|  |  |  |  |
|  | M03.D-M.1.2.2 <br> Add, subtract, multiply, and divide to solve one step word problems involving masses or liquid volumes that are given in the same units. |  |  |
|  | M03.D-M.1.2.3 <br> Use a ruler to measure lengths to the nearest quarter inch or centimeter. | M03DM1.2.3a | Use a ruler and measure to the nearest inch (exact measurement) |
| M03.D-M.1.3 <br> Count, compare, and make change using a collection of coins and one-dollar bills. | M03.D-M.1.3.1 <br> Compare total values of combinations of coins (penny, nickel, dime, and quarter) and/or dollar bills less than $\$ 5.00$. | M03DM1.3.1a | Count money using coins or onedollar bills |
|  | M03.D-M.1.3.2 <br> Make change for an amount up to $\$ 5.00$ with no more than $\$ 2.00$ change given (penny, nickel, dime, quarter, and dollar). |  |  |
|  | M03.D-M.1.3.3 <br> Round amounts of money to the nearest dollar. |  |  |

## PA Reporting Category: M03.D-M Measurement and Data

## PA Core Standards:

CC.2.4.3.A. 4 Represent and interpret data using tally charts, tables, pictographs, line plots, and bar graphs.

## ASSESSMENT ANCHOR

M03.D-M. 2 Represent and interpret data.

| DESCRIPTOR | ELIGIBLE CONTENT | Alternate Eligible <br> Content Code | ALTERNATE ELIGIBLE CONTENT |
| :--- | :--- | :--- | :--- |
| M03.D-M.2.1 <br> Organize, display, and <br> answer questions based <br> on data. | M03.D-M.2.1.1 <br> Complete a scaled pictograph and a scaled bar graph to <br> represent a data set with several categories (scales limited <br> to 1, 2, 5, and 10). | M03DM2.1.1a | Add information to a pictograph, <br> line plot, or bar graph |
|  | M03.D-M.2.1.2 <br> Solve one- and two-step problems using information to <br> interpret data presented in scaled pictographs and scaled <br> bar graphs (scales limited to 1, 2, 5, and 10). <br> Example 1: (One-step) "Which category is the largest?" <br> Example 2: (Two-step) "How many more are in category A <br> than in category B?" |  |  |
|  | M03.D-M.2.1.3 <br> Generate measurement data by measuring lengths using <br> rulers marked with halves and fourths of an inch. Display the <br> data by making a line plot, where the horizontal scale is <br> marked in appropriate units-whole numbers, halves, or <br> quarters. |  |  |
|  | M03.D-M.2.1.4 <br> Translate information from one type of display to another. <br> Limit to pictographs, tally charts, bar graphs, and tables. <br> Example: Convert a tally chart to a bar graph. |  |  |

## PA Reporting Category: M03.D-M Measurement and Data

## PA Core Standards:

CC.2.4.3.A. 5 Determine the area of a rectangle and apply the concept to multiplication and to addition.

## ASSESSMENT ANCHOR

M03.D-M. 3 Geometric measurement: understand concepts of area and relate area to multiplication and to addition.

| DESCRIPTOR | $\quad$ ELIGIBLE CONTENT | Alternate Eligible <br> Content Code | ALTERNATE ELIGIBLE CONTENT |
| :--- | :--- | :--- | :--- |
| M03.D-M.3.1 <br> Find the areas of plane <br> figures.M03.D-M.3.1.1 <br> Measure areas by counting unit squares (square cm, square <br> m, square in., square ft., and non-standard square units). |  |  |  |
|  | M03.D-M.3.1.2 <br> Multiply side lengths to find areas of rectangles with whole- <br> number side lengths in the context of solving real-world and <br> mathematical problems, and represent whole-number <br> products as rectangular areas in mathematical reasoning. | M03DM3.1.2a | Measure the area of a rectangle by <br> counting squares, tiling, or addition |

## PA Reporting Category: M03.D-M Measurement and Data

## PA Core Standards:

CC.2.4.3.A. 6 Solve problems involving perimeters of polygons and distinguish between linear and area measures.

## ASSESSMENT ANCHOR

M03.D-M. 4 Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures.

| DESCRIPTOR | ELIGIBLE CONTENT | Alternate Eligible <br> Content Code | ALTERNATE ELIGIBLE CONTENT |
| :--- | :--- | :--- | :--- |
| M03.D-M.4.1 <br> Find and use the <br> perimeters of plane <br> figures.M03.D-M.4.1.1 <br> Solve real-world and mathematical problems involving <br> perimeters of polygons, including finding the perimeter given <br> the side lengths, finding an unknown side length, exhibiting <br> rectangles with the same perimeter and different areas, and <br> exhibiting rectangles with the same area and different <br> perimeters. Use the same units throughout the problem. | M03DM4.1.1a | Find the perimeter of a rectangle |  |

