PA Core Standards: Mathematics

The most effective and equitable way to support students in their learning is to ensure that the vast majority of time is spent engaging with grade-level content, remediating with precision and accelerating as needed. It is entirely possible to hold high expectations for all students while addressing unfinished learning in the context of grade-level work. Since time is a scarce commodity in classroom, strategic instructional and assessment choices are critical.¹

Instruction
It is vitally important that educators are supported to make deliberate instructional choices that allow all students to effectively engage with grade-level work. Instruction must be aligned to a coherent set of learning outcomes, indicating what students should know and be able to do. Dimensions for consideration when planning for instruction include the following:

- **Delivery** is differentiated relative to explicitness through modeling, systematic instruction with appropriate scaffolding and pacing, and provision of immediate corrective feedback to students with sufficient opportunities to respond.
- **Grouping** includes whole group, homogeneous small group, partners, heterogeneous mixed ability small group, independent, and one-to-one.
- **Time** varies relative to a particular area of content, small group instruction versus whole group instruction, and opportunities for students to interact or work independently.
- **Materials** should be evidence-based and adjusted to meet the needs of students and the purpose of the lesson/activity.
- **Learning Environment** must be positive and safe and have clearly defined consistent expectations.

Assessment
A highly developed assessment system includes a balanced approach to using formal and informal assessments, classroom-based evidence showing growth over time, and involving students in the evaluation of their own work. The adoption of a systemic approach enhances the use of assessment data to inform teaching and learning practices. This system should include assessment tools that are congruent with the district's goals and curriculum. Assessments can be done in sync with daily instruction through intentional activities that can collect data to support instructional goals.

This guidance document is designed to identify areas of focus in Mathematics instruction, grade by grade. Each grade level guidance document defines high level focus of instruction, supported by PA Academic Standards. Note that while all standards deserve a defined level of instruction, neglecting key concepts may result in learning gaps in student skill and understanding and may leave students unprepared for the challenges of a later grade. Not all content in a given grade is emphasized equally in the standards. Some focus areas require greater emphasis then others based on the depth of the ideas, the time taken to master, and/or their importance to the future mathematics grade levels. More time in these areas is also necessary for students to meet the Standards for Mathematical Practice.

**Highlights of Focus Work, K-12**

| Grade K-2: Addition and subtraction – concepts, skills, and problem solving; place value | Grade 7: Ratios and proportional relationships; arithmetic of rational numbers |
| Grade 3-5: Multiplication and division of whole numbers and fractions - concepts, skills, and problem solving | Grade 8: Linear Algebra and functions |
| Grade 6: Ratios and proportional relationships; early expressions and equations | Grade HS: Course specific content area work |

For additional support and resources, contact PDE or your local Intermediate Unit. The resources listed below are provided as options and examples. Pennsylvania does not require, recommend, or endorse any specific program or product. All curricular and instructional decisions are made at the local level.

¹ Adapted from 2020–21 Priority Instructional Content in English Language Arts/literacy and Mathematics, Student Achievement Partners/Achieve the Core. May 2020
**Focus of Instruction: Numbers and Operations**

**Ratios, proportions, and percent:** Compute unit rates associated with ratios of fractions. Recognize and represent proportional relationships between quantities. Use proportional relationships to solve multistep ratio and percent problems.

**Rational Numbers:** Solve real-world and mathematical problems involving the four operations with rational numbers.

**Focus of Instruction: Algebraic Concepts**

**Algebraic expressions and equations:** Model and solve real-world and mathematical problems using multiple representations such as algebraic, graphical, and using tables. Solve multi-step equations or inequalities with one variable. Solve and interpret multi-step real life and mathematical problems posed with positive and negative rational numbers.

**Focus of Instruction: Geometry**

**Area, surface area, volume, angle measure, circumference:** Use properties of angle types and properties of angles formed when two parallel lines are cut by a transversal line to solve problems. Solve problems involving area and circumference of a circle(s). Solve mathematical problems involving area, volume, and surface area of two- and three-dimensional objects. Describe the two-dimensional figures that result from slicing three-dimensional figures.

**Focus of Instruction: Measurement, Data and Probability**

**Data, distributions, and random sampling:** Draw inferences about two populations based on random sampling concepts. Determine and approximate relative frequencies and probabilities of events. Find the probability of a simple event, including the probability of a simple event not occurring.

**Probability:** Find probabilities of independent compound events. Predict the approximate relative frequency given the probability.

**Classroom/Time Management**

Set high academic & behavioral expectations (students help establish guidelines).
Set the tone, establish a positive environment, & build relationships.
Establish procedures, routines, agenda, learning targets, & outcomes.
Model ideal behavior and use humor, positive language, proximity & nonverbal communication.
Encourage initiative, maintain student attention/engagement, & offer praise.
Make positive phone calls and send positive notes.
Rethink and arrange the class for maximum learning.
Balance lecturing and facilitating and establish peer teaching/tutoring.
Build classroom camaraderie with an activity, game, or tradition that is quirky, fun, and unique.
Employ empathy and understand trauma-informed care.

**Instructional Resources**

- SAS Online Resources for Instruction
- Mathematics Menu of Best Practices and Strategies
- SAS Search Standards (Assessment, Continuum of Activities, Materials & Resources)
- Math Teaching Strategies Videos
- The Learning Classroom: Theory into Practice (video series)
- Evidence-Based Specially Designed Instruction in Mathematics
- Research-Based Math Instructional Strategies

**Assessment Resources**

- Pennsylvania Classroom Diagnostic Tools (CDT) Resources
- SAS Assessment Builder
- PDE’s Assessment Data Protocol Process
- Basics on Assessments Systems
- FORMATIVE ASSESSMENT: 10 Key Questions
- Understanding Assessing Math (Short Videos)
- Depth of Knowledge with Karin Hess (video 23:16)

**Standards for Mathematics Practices**

- PA Core Standards, Standards for Mathematical Practice
- Mathematical Practice Standards
- Implementing the Standards of Mathematical Practices

**Classroom/Time Management Resources**

- Effective Lesson Planning, Delivery Techniques & Classroom Management Suggestions
- 5 Classroom Management Tips That Seem Counterintuitive
- Effective Classroom Management Strategies to Achieve Your Daily Goals
- 20 Classroom Management Strategies and Techniques
- 27 Classroom Management Strategies
- Classroom Management Strategies
- 5 Tips for Classroom Management in Middle and High School
- Classroom Management for Middle School and High School Teachers
- 50 Tips, Tricks, and Ideas for Teaching 7th Grade