9.1-9.3 POLYNOMIALS – ADDING, SUBTRACTING, AND MULTIPLYING

WHAT IS A POLYNOMIAL?

- A <u>polynomial</u> is an expression with multiple terms. It consists of constants, like -2 or 17, terms with variables, like 2x or -12m, and terms with exponents, like $-13n^2$. *Poly* means many and *nomial* means terms
- <u>Proper way to write a polynomial</u>: Terms in decreasing order, starting with the term with the biggest exponent(s).

• Examples: $3x^3 - x^2 + 1$ $2ab^4 + 4a^3b - a^2b$

<u>Degree of a polynomial</u>: the largest exponent in the polynomial

 <u>Leading Coefficient:</u> the coefficient on the very first term, when the polynomial is written in the proper order

WHAT ARE LIKE TERMS?

<u>Like terms</u> are terms that have the exact same variable(s), and the exact same exponent on the variable (s)

• Examples of like terms, and non-like terms:

Like terms	Unlike terms
$2x, -7x -8x^{2}, 3x^{2} 13xy, -7xy 5x^{2}y, 3x^{2}y x, 4x$	$2x, -7y -8x^{2}, 3x 13xy, -7xz 5x^{2}y, 3xy^{2} x, 4$

ADDING POLYNOMIALS

Drop the parentheses on both polynomials
 Combine like terms

• Exs) Find each sum.

• a.)
$$(3x^3 + 12x - 7x^2 - 20) + (14x + 4 - 2x^2)$$

• b.) $(17x^4 + 6 - 14x^2) + (10 - 5x^2 + 4x^3)$

SUBTRACTING POLYNOMIALS

- Drop the parentheses on ONLY the first polynomial, and rewrite below
 Distribute the negative throughout all terms in the second polynomial
 Combine like terms
- Exs) Find each difference.
- d.) $(12a^3 + 11a 24) (3a^3 4a^2 + 14a 1)$

1)
$$(x^{3} + 7 - 7x) + (7x^{4} - 3x - 6)$$

2) $(6n + 6n^{2} + 6n^{4}) + (n + 8n^{4} + 7n^{2})$
3) $(3 - 5x^{2} + 4x^{4}) - (8 - 2x^{2} + 3x)$
4) $(6n^{2} - 3 + 3n) - (3n^{2} + 3n - 5)$

MULTIPLYING POLYNOMIALS

- 1.) Multiply each term in the first polynomial by each term in the second polynomial (multiply coefficients, and add exponents on variable that are the same)
- 2.) Simplify by combining like terms
- Exs) g.) $2x^2(3x^4 6x^3 + 4)$ h.) (6y - 2)(y + 1)i.) $(2b^2 + 5)(b^3 + 3)$

• j.) (c-2)(c+4) k.) $(2x-1)(3x^2-x+4)$ l.) $(2x-3)^2$