# Graphs of Secant, Cosecant, Tangent, and Cotangent <br> Graphs of Secant and Cosecant 

## Cosecant:

Cosecant is the reciprocal of sine $\rightarrow$ if sine has a max value of 1 , cosecant will have a min value at 1 ; if sine has a min value of -1 , cosecant will have a max value at -1 , etc


## Secant:

Secant is the reciprocal of cosine $\rightarrow$ if cosine has a max value of 1 , secant will have a min value at 1 ; if cosine has a min value of -1 , secant will have a max value at -1 , etc

$\leftarrow$ vertical asymptotes (dashed lines) where the sine function touches the x axis

## Tangent:

Characteristics of the graph of $y=\tan (x)$ :

- There are vertical asymptotes wherever tangent is undefined [wherever $\cos (x)=0$ since $\tan (\mathrm{x})=\sin (\mathrm{x}) / \cos (\mathrm{x})] \leftarrow$ graph will never touch/cross these asymptotes
- The period is $\pi$ (this is because if you look at the unit circle, the values of tangent repeat themselves every half revolution, or $\pi$ revolutions)
- Domain: all real numbers except where the asymptotes occur
- Range: all real numbers
- No amplitude

- Between 0 and $\frac{\pi}{2}$ sine and cosine are both positive $\rightarrow$ tangent is positive
- Between $\frac{\pi}{2}$ and $\pi$ sine is positive but cosine is negative $\rightarrow$ tangent is negative
- Between $\pi$ and $\frac{3 \pi}{2}$ sine is negative and cosine is negative $\rightarrow$ tangent is positive
- Between $\frac{3 \pi}{2}$ and $2 \pi$ sine is negative and cosine is positive $\rightarrow$ tangent is negative


## Cotangent:

Cotangent is the reciprocal of tangent $\rightarrow$ While the graph of $y=\tan (x)$ has vertical asymptotes where $\cos (x)=0, y=\cot (x)$ has vertical asymptotes where $\sin (x)=0[$ since $\cot (x)=\cos (x) / \sin (x)]$

Same rules apply to construct the graph as we did $y=\tan (x) \rightarrow$ check to see what the sigh of cot is based upon the sign of $\sin$ and $\cos$ on that interval (quadrant)

$$
y=\cot (x)
$$



- Between 0 and $\frac{\pi}{2}$ sine and cosine are both positive $\rightarrow$ cotangent is positive
- Between $\frac{\pi}{2}$ and $\pi$ sine is positive but cosine is negative $\rightarrow$ cotangent is negative
- Between $\pi$ and $\frac{3 \pi}{2}$ sine is negative and cosine is negative $\rightarrow$ cotangent is positive
- Between $\frac{3 \pi}{2}$ and $2 \pi$ sine is negative and cosine is positive $\rightarrow$ cotangent is negative

