

You must show all of your work to get credit on the test.

If $\sin u = \frac{3}{5}$, $\frac{\pi}{2} < u < \pi$, and $\cos v = \frac{8}{17}$, $\frac{2\pi}{3} < v < 2\pi$, find the exact value of the following.

1. $\sin 2u$

2. $\csc(u - v)$

3. $\cot 2v$

Find the exact value of each.

4. $\sin(75^\circ)$

5. $\sin(330^\circ) \cos(30^\circ) - \cos(330^\circ) \sin(30^\circ)$

6. Use power-reducing-formulas to write $[\sin^2(x)] \cos^2(x)$ in terms of a first power cosine.

7. Use product-to-sum formulas to write $\cos 2x \sin 4x$ as a sum or difference.

8. Use sum-to-product formulas to find the exact value of $\sin 105^\circ - \sin 15^\circ$

Solve $[0, 2\pi)$. **CHOOSE 5 OF THE 6** and circle them so I know which you want graded.

1. $\csc^2(x) - \sqrt{2} \csc(x) = 0$

2. $\sin(2x) = \cos(x)$

3. $\tan^2 x + \sec x = 1$

4. $5\sin^2 x - 4 \sin x - 1 = 0$

5. $2 \cos 2x \sin x - \sqrt{3} \sin x = 0$

6. $2 \sin^2(x) + \sin(x) = 0$

Verify. **CHOOSE 5 OF THE 6** and circle them so I know which you want graded. 4 points each.

1. $\cos^2(x) + \cos^2(x) \tan^2(x) = 1$

2. $\frac{1}{1-\sin(x)} + \frac{1}{1+\sin(x)} = 2 \sec^2(x)$

3. $\tan(x) \csc(x) = \sec(x)$

4. $\frac{\tan^2(x)+1}{1+\cot^2(x)} = \tan^2(x)$

5. $\frac{2 \sin^2(x)-1}{\sin(x) \cos(x)} = \tan(x) - \cot(x)$

6. $\sin(x)[\csc(x) - \sin(x)] = \cos^2(x)$

7. $\frac{1-\sin^2(x)}{\csc^2(x)-1} = \sin^2(x)$

8. $\tan^2(x) - \tan^2(x) \sin^2(x) = \sin^2(x)$

9. $\frac{\sin(x)}{1-\cos(x)} + \frac{1-\cos(x)}{\sin(x)} = 2 \csc(x)$

10. $\cos(x) + \sin(x) \tan(x) = \sec(x)$

$$\sin^2 u = \frac{1 - \cos 2u}{2}$$

$$\cos^2 u = \frac{1 + \cos 2u}{2}$$

$$\tan^2 u = \frac{1 - \cos 2u}{1 + \cos 2u}$$

$$\sin u \sin v = \frac{1}{2} [\cos(u - v) - \cos(u + v)] \quad \cos u \cos v = \frac{1}{2} [\cos(u - v) + \cos(u + v)]$$

$$\sin u \cos v = \frac{1}{2} [\sin(u + v) + \sin(u - v)] \quad \cos u \sin v = \frac{1}{2} [\sin(u + v) - \sin(u - v)]$$

$$\sin u + \sin v = 2 \sin\left(\frac{u+v}{2}\right) \cos\left(\frac{u-v}{2}\right)$$

$$\sin u - \sin v = 2 \cos\left(\frac{u+v}{2}\right) \sin\left(\frac{u-v}{2}\right)$$

$$\cos u + \cos v = 2 \cos\left(\frac{u+v}{2}\right) \cos\left(\frac{u-v}{2}\right)$$

$$\cos u - \cos v = -2 \sin\left(\frac{u+v}{2}\right) \sin\left(\frac{u-v}{2}\right)$$