

**3-1 Study Guide and Intervention****Graphing Linear Equations**

**Identify Linear Equations and Intercepts** A **linear equation** is an equation that can be written in the form  $Ax + By = C$ . This is called the **standard form** of a linear equation.

**Standard Form of a Linear Equation**

$Ax + By = C$ , where  $A \geq 0$ ,  $A$  and  $B$  are not both zero, and  $A$ ,  $B$ , and  $C$  are integers with a greatest common factor of 1

**Example 1**

**Determine whether  $y = 6 - 3x$  is a linear equation. Write the equation in standard form.**

First rewrite the equation so both variables are on the same side of the equation.

$$y = 6 - 3x$$

Original equation

$$y + 3x = 6 - 3x + 3x$$

Add  $3x$  to each side.

$$3x + y = 6$$

Simplify.

The equation is now in standard form, with  $A = 3$ ,  $B = 1$  and  $C = 6$ . This is a linear equation.

**Example 2**

**Determine whether  $3xy + y = 4 + 2x$  is a linear equation. Write the equation in standard form.**

Since the term  $3xy$  has two variables, the equation cannot be written in the form  $Ax + By = C$ . Therefore, this is not a linear equation.

**Exercises**

**Determine whether each equation is a linear equation. Write *yes* or *no*. If yes, write the equation in standard form.**

1.  $2x = 4y$

2.  $6 + y = 8$

3.  $4x - 2y = -1$

4.  $3xy + 8 = 4y$

5.  $3x - 4 = 12$

6.  $y = x^2 + 7$

7.  $y - 4x = 9$

8.  $x + 8 = 0$

9.  $-2x + 3 = 4y$

10.  $2 + \frac{1}{2}x = y$

11.  $\frac{1}{4}y = 12 - 4x$

12.  $3xy - y = 8$

13.  $6x + 4y - 3 = 0$

14.  $yx - 2 = 8$

15.  $6x - 2y = 8 + y$

16.  $\frac{1}{4}x - 12y = 1$

17.  $3 + x + x^2 = 0$

18.  $x^2 = 2xy$

**3-1 Study Guide and Intervention** *(continued)***Graphing Linear Equations**

**Graph Linear Equations** The graph of a linear equation represents all the solutions of the equation. An  $x$ -coordinate of the point at which a graph of an equation crosses the  $x$ -axis is an  **$x$ -intercept**. A  $y$ -coordinate of the point at which a graph crosses the  $y$ -axis is called a  **$y$ -intercept**.

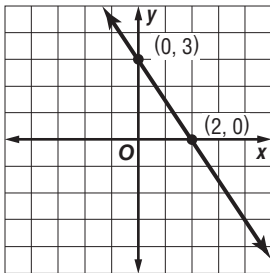
**Example 1** Graph  $3x + 2y = 6$  by using the  $x$ - and  $y$ -intercepts.

To find the  $x$ -intercept, let  $y = 0$  and solve for  $x$ . The  $x$ -intercept is 2. The graph intersects the  $x$ -axis at  $(2, 0)$ .

To find the  $y$ -intercept, let  $x = 0$  and solve for  $y$ .

The  $y$ -intercept is 3. The graph intersects the  $y$ -axis at  $(0, 3)$ .

Plot the points  $(2, 0)$  and  $(0, 3)$  and draw the line through them.



**Example 2** Graph  $y - 2x = 1$  by making a table.

Solve the equation for  $y$ .

$$\begin{aligned} y - 2x &= 1 \\ y - 2x + 2x &= 1 + 2x \\ y &= 2x + 1 \end{aligned}$$

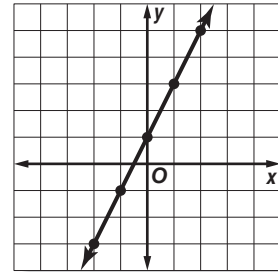
Original equation

Add  $2x$  to each side.

Simplify.

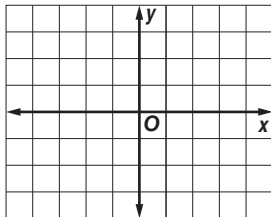
Select five values for the domain and make a table. Then graph the ordered pairs and draw a line through the points.

$x$	$2x + 1$	$y$	$(x, y)$
-2	$2(-2) + 1$	-3	$(-2, -3)$
-1	$2(-1) + 1$	-1	$(-1, -1)$
0	$2(0) + 1$	1	$(0, 1)$
1	$2(1) + 1$	3	$(1, 3)$
2	$2(2) + 1$	5	$(2, 5)$

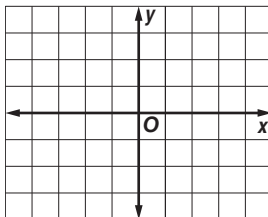
**Exercises**

Graph each equation by using the  $x$ - and  $y$ -intercepts.

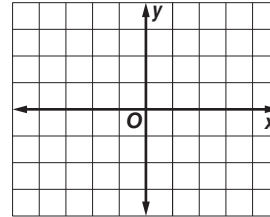
1.  $2x + y = -2$



2.  $3x - 6y = -3$

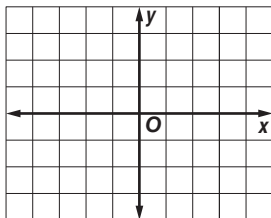


3.  $-2x + y = -2$

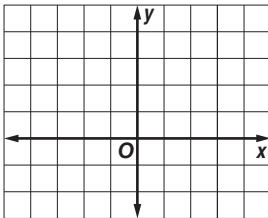


Graph each equation by making a table.

4.  $y = 2x$



5.  $x - y = -1$



6.  $x + 2y = 4$

